

Lecture 8 Summary and Conclusions

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Last slide from Lect. 1

Goal of Course

Understanding of the role of electrons in condensed matter

- **Practical, useful knowledge** of methods that are working tools of theorists, experimentalists, and researchers in many fields

Without the burden of heavy math, many-body theory,

- **Appreciation** for the real many-body problems presented by electrons in condensed matter

Understanding when to expect correlation to be important
The grand challenges of condensed matter physics today

For those who are interested

- **Practical, useful knowledge** of **many-body** methods that are becoming more and more important for quantitative predictions and understanding the grand challenges in condensed matter

Basis of Most Modern Calculations Density Functional Theory

- Why is Density Functional Theory so widely used?
- A new approach to the many-body interacting electron problem
 - In principle DFT is exact
 - Kohn and Sham introduced the idea of an auxiliary system that in principle gives the exact ground state density and energy - but NOT other properties.
 - In practice, DFT allows useful approximations

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The Car-Parrinello Advance

- **Car-Parrinello Method – 1985**
 - Simultaneous solution of Kohn-Sham equations for electrons and Newton's equations for nuclei
- A revolution in the power of the methods
 - Relaxation of positions of nuclei to find structures
 - "First principles" molecular dynamics simulations of solids and liquids with nuclei moving thermally
 - Chemical reactions, . . .
- Stimulated further developments

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Contents of a typical solid state physics text (Kittel, Ashcroft and Mermin,)

From Lect. 1

- **Structures of crystals**
 - Definitions of structures
 - Typical bonding and structures
 - Structural phase transitions
- **Mechanical Properties**
 - Lattice vibrations – phonons
 - Elastic constants
 - Piezoelectric constants
 - Effective charges
- **Thermal Properties**
 - Heat capacity, heat conduction
- **Electronic properties**
 - Definition of bands
 - Metals vs. insulators
 - Conductivity, dielectric functions
 - Magnetism

Properties that can be described without knowing anything about electrons

Did we answer the question:
Why are they a part of electronic structure?

Properties that can only be understood in terms of the electrons?

So what is left to do?

- **Failures of present density functional approximations in important cases!**
- **Electronic excitations**
 - The “band gap problem” . . .
- **Strongly interacting systems**
 - Magnetic insulators, metal-insulator transitions, . . .
- **Example of “Failure” that has been solved!**
 - Weak Van der Waals bonds
 - Development of non-local functional has the right distance dependence and is accurate enough for real materials
- **Very brief presentation in special lectures**

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From Lect. 1 modified

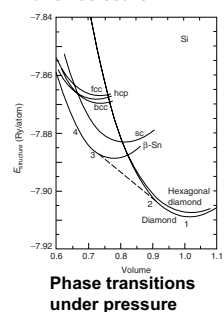
Useful!

Treat many types of materials in a unified way from the basic equations

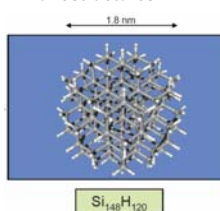
Calculate properties of Crystals



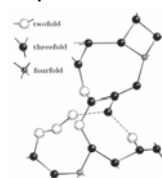
Predict crystal structures
Example – atomic positions in a ferroelectric



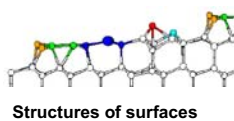
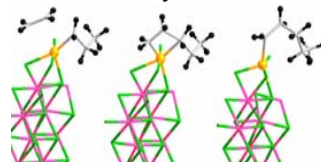
Predict properties of nanostructures



Simulation of Liquids – example Carbon at high T



Reactions – catalysis at a surface



Many other examples!

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Not covered due to time constraint

Magnetism

Wannier functions – transformation from extended Bloch states to localized orbitals

Linear scaling methods – using Wannier functions

Electric polarization in solids – using Wannier functions (or Berry phases)

Excitations and time dependent density functional theory

Magnetism

The good thing about magnetism

Simple models give the right qualitative understanding

Atom-like magnetic moments

Ordered for $T < T_c$ -- disordered for $T > T_c$

Another good thing about magnetism

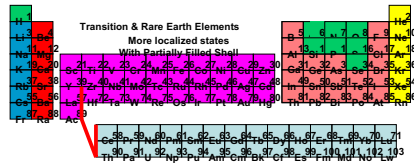
Simple models give the right qualitative understanding

Electrons in bands

Magnetic moment is $n_{\text{up}} - n_{\text{down}}$

The hard thing about the theory of magnetism

To understand both these pictures at the same time!



“Order N”

Quantum Mechanics is not “local”

Eigenstates extend over entire system

Interference of states is essential to understanding quantum behavior

Effect in theoretical calculations for materials

Exact calculations - Computer time scales exponentially with N = number of electrons

In DFT – scales as N^3 (The time to diagonalize a matrix)

Is it possible to do accurate calculations with computational time linear in N ?

Wannier functions

Transformation from an entire band of Bloch states to a set of Wannier functions

Zone center
 $k = 0$



Extended
Bloch
Eigenstates

Zone boundary
 $k = \pi/a$

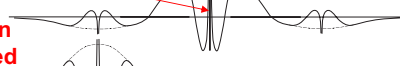


Wannier function
 $W(x - T_0)$ centered
in cell 0



Localized Wannier
functions

Wannier function
 $W(x - T_{-1})$ centered
in cell -1



NOT eigenstates

Each function is
a linear combination
of eigenstates

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